## The Pennsylvania System of School Assessment

## Mathematics Item and Scoring Sampler



2017-2018
Grade 7
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## INTRODUCTION

## General Introduction

The Pennsylvania Department of Education provides districts and schools with tools to assist in delivering focused instructional programs aligned with the Pennsylvania Core Standards (PCS). These tools include Academic Standards, Assessment Anchor documents, assessment handbooks, and content-based item and scoring samplers. This Item and Scoring Sampler is a useful tool for Pennsylvania educators in preparing local instructional programs. It can also be useful in preparing students for the statewide assessment.

This Item and Scoring Sampler is available in Braille format. For more information regarding Braille call (717) 901-2238.

## PennsyIvania Core Standards (PCS)

This sampler contains examples of test questions designed to assess the Pennsylvania Assessment Anchors and Eligible Content aligned to the Pennsylvania Core Standards. The Mathematics, Reading, and Writing PSSA transitioned to PCS-based operational Mathematics and English Language Arts assessments starting with the spring 2015 PSSA administration.

The 2013 PCS-aligned Assessment Anchor and Eligible Content documents are posted on this portal:
> www.education.pa.gov [Hover over "K-12," select "Assessment and Accountability," and select "Pennsylvania System of School Assessment (PSSA)." Then select "Assessment Anchors/Eligible Content" on the right side of the screen.]

## What Is Included

This sampler contains test questions (items) that have been written to align to the Assessment Anchors that are based on the Pennsylvania Core Standards (PCS). The test questions provide an idea of the types of items that will appear on an operational, PCS-based PSSA. Each sample test question has been through a rigorous review process to ensure alignment with the Assessment Anchors.

## Purpose and Uses

The items in this sampler may be used as examples for creating assessment items at the classroom level, and they may also be copied and used as part of a local instructional program. ${ }^{1}$ Classroom teachers may find it beneficial to have students respond to the open-ended item in this sampler. Educators can then use the sampler as a guide to score the responses either independently or together with colleagues within a school or district.

## Item Format and Scoring Guidelines

The multiple-choice (MC) items have four answer choices. Each correct response to an MC item is worth one point.
Each open-ended (OE) item is designed to take approximately ten to fifteen minutes to complete. During the administration of the PSSA, students are given additional time as necessary to complete the test items. Each OE item in mathematics is scored using an item-specific scoring guideline based on a $0-4$-point scale. In this sampler, every item-specific scoring guideline is combined with examples of student responses that represent each score point to form a practical, item-specific scoring guide.

This sampler also includes the General Description of Scoring Guidelines for Mathematics Open-Ended Questions that students will have access to during a PSSA mathematics administration. The general description of scoring guidelines can be distributed to students for use during local assessments and can also be used by educators when scoring local assessments. ${ }^{1}$

[^0]
## Item Alignment

All PSSA items are aligned to statements and specifications included in the Assessment Anchors and Eligible Content Aligned to the Pennsylvania Core Standards. The mathematics content, process skills, directives, and action statements included in the PSSA mathematics questions align with the Assessment Anchor Content Standards. The Eligible Content statements represent the limits of the content of the mathematics questions.

## Testing Time and Mode of Testing Delivery for the PSSA

The PSSA is delivered in traditional paper-and-pencil format as well as in an online format. The estimated time to respond to a test question is the same for both methods of test delivery. During an official testing administration, students are given additional time as necessary to complete the test questions. The following table shows the estimated response time for each item type.

| Mathematics Item Type | MC | OE |
| :---: | :---: | :---: |
| Estimated Response Time <br> (minutes) | 2 | 10 to 15 |

## Mathematics Reporting Categories

The Assessment Anchors are organized into four classifications as listed below.

| $-\mathrm{A}=$ Numbers and Operations | $\bullet$ C = Geometry |
| :--- | :--- |
| $\bullet$ B = Algebraic Concepts | $\bullet$ D = Data Analysis and Probability |

These four classifications are used throughout the grade levels. In addition to these classifications, there are five Reporting Categories for each grade level. The first letter of each Reporting Category represents the classification; the second letter represents the Domain as stated in the Common Core State Standards for Mathematics. Listed below are the Reporting Categories for Grade 7.

- $\mathrm{A}-\mathrm{N}=$ The Number System
- A-R = Ratios and Proportional Relationships
- $B-E=$ Expressions and Equations
- C-G = Geometry
- D-S = Statistics and Probability

Examples of multiple-choice and open-ended items assessing these categories are included in this booklet.

## General Description of Scoring Guidelines for Mathematics Open-Ended Questions

4- The response demonstrates a thorough understanding of the mathematical concepts and procedures required by the task.

The response provides correct answer(s) with clear and complete mathematical procedures shown and a correct explanation, as required by the task. Response may contain a minor "blemish" or omission in work or explanation that does not detract from demonstrating a thorough understanding.

3- The response demonstrates a general understanding of the mathematical concepts and procedures required by the task.

The response and explanation (as required by the task) are mostly complete and correct. The response may have minor errors or omissions that do not detract from demonstrating a general understanding.

2- The response demonstrates a partial understanding of the mathematical concepts and procedures required by the task.

The response is somewhat correct with partial understanding of the required mathematical concepts and/or procedures demonstrated and/or explained. The response may contain some work that is incomplete or unclear.

1- The response demonstrates a minimal understanding of the mathematical concepts and procedures required by the task.

0 - The response has no correct answer and insufficient evidence to demonstrate any understanding of the mathematical concepts and procedures required by the task for that grade level.

Response may show only information copied from the question.
Special Categories within zero reported separately:
BLK (blank) $\qquad$ Blank, entirely erased, or written refusal to respond
OT. $\qquad$ .Off task

LOE. $\qquad$ Response in a language other than English
IL $\qquad$ Illegible

## Item and Scoring Sampler Format

This sampler includes the test directions and scoring guidelines that appear in the PSSA Mathematics assessments. Each multiple-choice item is followed by a table that includes the alignment, the answer key, the depth of knowledge (DOK) level, the percentage ${ }^{2}$ of students who chose each answer option, and a brief answer-option analysis or rationale. The open-ended item is followed by a table that includes the item alignment, DOK level, and mean student score. Additionally, each of the included item-specific scoring guidelines is combined with sample student responses representing each score point to form a practical, item-specific scoring guide. The General Description of Scoring Guidelines for Mathematics Open-Ended Questions used to develop the item-specific scoring guidelines should be used if any additional item-specific scoring guidelines are created for use within local instructional programs.

Example Multiple-Choice Item Information Table

| Item Information | Assigned AAEC |
| :--- | :--- |
| Alignment | Correct Answer |
| Answer Key | Assigned DOK |
| Depth of Knowledge | Percentage of students who selected each option |
| $p$-value A | Percentage of students who selected each option |
| $p$-value B | Percentage of students who selected each option |
| $p$-value C | Percentage of students who selected each option |
| $p$-value D | Brief answer-option analysis or rationale |
| Option Annotations |  |
|  |  |

Example Open-Ended Item Information Table

| Alignment | Assigned AAEC | Depth of Knowledge | Assigned DOK | Mean Score |  |
| :--- | :--- | :--- | :--- | :--- | :--- |

[^1]
## Grade 7 Formula Sheet

Formulas that you may need to work questions on this test are found below.
You may refer back to this page at any time during the mathematics test.

## Simple Interest

$$
I=P r t
$$

## Circle



$$
C=2 \pi r \quad A=\pi r^{2}
$$

Triangle

$A=\frac{1}{2} b h$

Square


$$
A=s^{2}
$$


$A=l w$
$P=2 l+2 w$


$$
A=b h
$$

## Trapezoid



$$
A=\frac{1}{2} h\left(b_{1}+b_{2}\right)
$$

## Rectangular Prism



$$
V=l w h \quad S A=2 l w+2 l h+2 w h
$$

## Polygonal Prism


$V=B w$, where $B=$ area of the base
$S A=P w+2 B$, where $P=$ perimeter of base

## Mathematics Test Directions

On the following pages are the mathematics questions.

- You may not use a calculator for question 1. You may use a calculator for all other questions on this test.


## Directions for Multiple-Choice Questions:

Some questions will ask you to select an answer from among four choices.
For the multiple-choice questions:

- First solve the problem on scratch paper.
- Choose the correct answer and record your choice in the answer booklet.
- If none of the choices matches your answer, go back and check your work for possible errors.
- Only one of the answers provided is the correct response.


## Directions for Open-Ended Questions:

Some questions will require you to write your response.
For the open-ended questions:

- These questions have more than one part. Be sure to read the directions carefully.
- You cannot receive the highest score for an open-ended question without completing all tasks in the question. For example, if the question asks you to show your work or explain your reasoning, be sure to show your work or explain your reasoning in the space provided.
- If the question does not ask you to show your work or explain your reasoning, you may use the space provided, but only those parts of your response that the question specifically asks for will be scored.
- Write your response in the appropriate location within the response box in the answer booklet. Some answers may require graphing, plotting, labeling, drawing, or shading. If you use scratch paper, be sure to transfer your final response and any needed work or reasoning to the answer booklet.


## Question 1 in this sampler is to be solved without the use of a calculator.

## MULTIPLE-CHOICE ITEMS

1. Multiply: $1 \frac{3}{7} \bullet \frac{-3}{7}$
A. $-4 \frac{2}{7}$
B. $-2 \frac{2}{7}$
C. $\frac{-30}{49}$
D. 1

## Item Information

| Alignment | A-N.1.1.3 |
| :--- | :--- |
| Answer Key | C |
| Depth of Knowledge | $14 \%$ |
| $p$-value A | $22 \%$ |
| $p$-value B | $47 \%$ (correct answer) |
| $p$-value C | $17 \%$ |
| $p$-value D | A. correctly sets up as $\frac{10}{7} \bullet \frac{-3}{7}$ but only multiplies numerators because of the <br> Option Annotations <br>  <br>  <br> B. multiplies fractional parts $\left(\frac{3}{7} \bullet \frac{3}{7}\right)$ but only multiplies numerators because of <br> the common denominator, adds $1+\left(1 \frac{2}{7}\right)$, and then makes the sum negative <br> C. correct <br> D. subtracts fractional parts $\left\langle\frac{3}{7}-\frac{3}{7}\right)$, leaving only whole number |

## A calculator is permitted for use in solving questions 2-17 in this sampler.

2. The price of a company stock that Meredith owns is $\$ 31.89$ on the morning of day 1 . At the end of each day for five days, Meredith records the change in the price of the stock. The changes she records are shown in the chart below, but some information is missing.

## Meredith's Stock

| Day | Change in <br> Price (\$) |
| :---: | :---: |
| 1 | +0.13 |
| 2 |  |
| 3 | -0.45 |
| 4 | +0.37 |
| 5 |  |

The change in the price for day 2 is $\frac{1}{3}$ of the change in the price for day 3 . At the end of day 5 , the price of Meredith's stock is $\$ 32.05$. What is the change, in dollars, in the price of the stock for day 5 ?
A. -0.04
B. +0.11
C. +0.16
D. +0.26

Item Information

| Alignment | A-N.1.1 |
| :--- | :--- |
| Answer Key | D |
| Depth of Knowledge | 2 |
| $p$-value A | $15 \%$ |
| $p$-value B | $17 \%$ |
| $p$-value C | $27 \%$ |
| $p$-value D | $41 \%$ (correct answer) |
| Option Annotations | A. makes a sign error on day 2 and uses +0.15 for change in price for day 2 <br> B. ignores day 2 information (i.e., treats as no change) <br> C. determines the total change in price from day 1 to day 5 (32.05 - 31.89) <br> D. correct |

## PSSA MATHEMATICS GRADE 7

3. Jellybeans cost $\$ 0.80$ per pound. Howard buys $4 \frac{1}{2}$ pounds of jellybeans for himself and

1 pound for his friend. What is the total cost of the jellybeans Howard buys?
A. $\$ 4.00$
B. $\$ 4.40$
C. $\$ 4.50$
D. $\$ 4.60$

## Item Information

| Alignment | A-N.1.1.1 <br> A-N.1.1.3 |
| :--- | :--- |
| Answer Key | B |
| Depth of Knowledge | 2 |
| $p$-value A | $8 \%$ |
| $p$-value B | $70 \%$ (correct answer) |
| $p$-value C | $10 \%$ |
| $p$-value D | $12 \%$ |
| Option Annotations | A. adds 1 to numerator of fraction instead of to whole number |
|  | B. correct |
|  | C. multiplies 5 by $\$ 0.80$ and then adds $\$ 0.50$ for the $\frac{1}{2}$ |

## PSSA MATHEMATICS GRADE 7

4. Which number line represents $-6-5$ ?
A.

B.

C.

D.


Item Information

| Alignment | A-N.1.1.2 |
| :--- | :--- |
| Answer Key | A |
| Depth of Knowledge | 2 |
| $p$-value A | $63 \%$ (correct answer) |
| $p$-value B | $16 \%$ |
| $p$-value C | $3 \%$ |
| $p$-value D | $18 \%$ |
| Option Annotations | A. correct <br> B. goes to -6 and then subtracts 5 by going 5 in the opposite direction <br> C. goes to 6 first and then subtracts 5 <br> D. goes to -6 in one direction and to 5 in the opposite direction |

## PSSA MATHEMATICS GRADE 7

5. Coach Patrick is ordering football jerseys for his team. The table below shows the relationship between the number of jerseys ordered and the total cost of the jerseys.

Football Jerseys

| Number <br> of Jerseys | Total Cost <br> (\$) |
| :---: | :---: |
| 10 | 75 |
| 20 | 150 |
| 30 | 225 |
| 40 | 300 |

Based on the information shown in the table, what is the total cost of ordering 52 jerseys?
A. $\$ 352$
B. $\$ 375$
C. $\$ 390$
D. $\$ 450$

| Item Information | A-R.1.1 |
| :--- | :--- |
| Alignment | C |
| Answer Key | 2 |
| Depth of Knowledge | $5 \%$ |
| $p$-value A | $15 \%$ |
| $p$-value B | $73 \%$ (correct answer) |
| $p$-value C | $7 \%$ |
| $p$-value D | A. adds 52 to the last total cost in the table <br> B. extends total cost to next expected entry in table (i.e., uses rule "add 75 ") <br> C. correct <br> D. adds $75 \times 2$ to the last total cost in the table |
| Option Annotations |  |

6. A turtle traveled $\frac{1}{10}$ mile in $\frac{1}{2}$ hour. What was the turtle's rate in miles per hour?
A. $\frac{1}{20}$
B. $\frac{1}{12}$
C. $\frac{1}{6}$
D. $\frac{1}{5}$

## Item Information

| Alignment | A-R.1.1.1 |
| :--- | :--- |
| Answer Key | D |
| Depth of Knowledge | 2 |
| $p$-value A | $28 \%$ |
| $p$-value B | $6 \%$ |
| $p$-value C | $4 \%$ |
| $p$-value D | $62 \%$ (correct answer) |
| Option Annotations | A. multiplies $\frac{1}{10}$ and $\frac{1}{2}$ |
|  | B. adds the denominators |
|  | C. adds the numerators and denominators and simplifies $\frac{2}{12}$ |

7. The graph below shows the relationship between the number of pounds of bananas purchased and the cost of the bananas. Four points on the graph are labeled.

Banana Cost


Based on the graph, which statement about the unit price of the bananas is true?
A. Point $Z$ indicates that the unit price is $\$ 0.00$ per pound.
B. Together, point $W$ and point $X$ indicate that the unit price is $\$ 0.50$ per pound.
C. Point $Y$ indicates that the unit price is $\$ 0.60$ per pound.
D. Together, point $X$ and point $Z$ indicate that the unit price is $\$ 2.40$ per pound.

## Item Information

| Alignment | A-R.1.1.5 |
| :--- | :--- |
| Answer Key | C |
| Depth of Knowledge | 2 |
| $p$-value A | $11 \%$ |
| $p$-value B | $8 \%$ |
| $p$-value C | $74 \%$ (correct answer) |
| $p$-value D | $7 \%$ |
| Option Annotations | A. interprets the value of the $y$-intercept as the rate of change <br> B. calculates $(1.80+1.20) \div(3 \times 2)$ as the rate of change <br> C. correct <br> D. calculates $(1.20-0) \times(2-0)$ as the rate of change |

## PSSA MATHEMATICS GRADE 7

8. A principal buys $x$ small tables and $y$ large tables for a computer lab.

- Each small table costs \$34.
- Each large table costs \$52.
- $\quad$ The total cost of the tables is less than $\$ 3,500$.
- The principal buys fewer than 50 tables.

Which two inequalities could represent this situation?
A. $34 x+52 y<3,500$
$x+y<50$
B. $34 x+52 y<3,500$
$x+y>50$
C. $52 x+34 y<3,500$
$x+y<50$
D. $52 x+34 y<3,500$
$x+y>50$

Item Information

| Alignment | B-E.2.2 |
| :--- | :--- |
| Answer Key | A |
| Depth of Knowledge | 2 |
| $p$-value A | $52 \%$ (correct answer) |
| $p$-value B | $24 \%$ |
| $p$-value C | $14 \%$ |
| $p$-value D | $10 \%$ |
| Option Annotations | A. correct <br> B. reverses the direction of the inequality for the second inequality <br> C. reverses the coefficients for the first inequality <br> D. reverses the coefficients for the first inequality and reverses the direction of <br> the inequality for the second inequality |

## PSSA MATHEMATICS GRADE 7

9. Nadia is selling tickets for a school event. She has already sold 17 tickets. Her goal is to sell at least 100 tickets. Each day she is able to sell up to 10 tickets. What is the minimum number of days Nadia will need to sell tickets to reach her goal?
A. 5
B. 6
C. 8
D. 9

| Item Information | B-E.2.2.2 <br> B-E.2.3.1 |
| :--- | :--- |
| Alignment | D |
| Answer Key | 2 |
| Depth of Knowledge | $9 \%$ |
| $p$-value A | $9 \%$ |
| $p$-value B | $23 \%$ |
| $p$-value C | $59 \%$ (correct answer) |
| $p$-value D | A. sets up equation as $100=17 x+10$, solves for $x$, and rounds down <br> B. sets up equation as $100=17 x+10$, solves for $x$, and (correctly) rounds up <br> C. correctly solves for $x$ but then rounds down <br> D. correct |
| Option Annotations |  |

## PSSA MATHEMATICS GRADE 7

10. A scale drawing of a triangle that will be used on a banner is shown below.


6 in.
What is the perimeter, in feet, of the actual triangle used on the banner?
A. $20 \frac{1}{2}$
B. 24
C. $25 \frac{1}{2}$
D. 27

Item Information

| Alignment | C-G.1.1.1 <br> C-G.1.1.2 |
| :--- | :--- |
| Answer Key | B |
| Depth of Knowledge | 2 |
| $p$-value A | $17 \%$ |
| $p$-value B | $61 \%$ (correct answer) |
| $p$-value C | $15 \%$ |
| $p$-value D | $7 \%$ |
| Option Annotations | A. applies scale by adding $1 \frac{1}{2}$ to each side length |
|  | C. recognizes triangle is isosceles but uses 6 in., 6 in., 5 in. as the side lengths <br> D. does not recognize triangle is isosceles and makes unknown side longer <br> than the others by using 5 in., 6 in., 7 in. as the side lengths |

11. Barb has a jewelry box in the shape of a rectangular pyramid. The top opens at a cross section parallel to the base.


What is the shape of the opening of the jewelry box?
A. rectangle
B. rhombus
C. trapezoid
D. triangle

Item Information

| Alignment | C-G.1.1.4 |
| :--- | :--- |
| Answer Key | A |
| Depth of Knowledge | 1 |
| $p$-value A | $48 \%$ (correct answer) |
| $p$-value B | $15 \%$ |
| $p$-value C | $11 \%$ |
| $p$-value D | $26 \%$ |
| Option Annotations | A. correct <br> B. misidentifies sides of cross section as being congruent and may not <br> recognize angle measures of cross section must be right angles (to match <br> parallel face) |

## PSSA MATHEMATICS GRADE 7

12. Two parallel lines are intersected by another line, as shown below.


What is the measure of $\angle 1$ ?
A. $61^{\circ}$
B. $74^{\circ}$
C. $81^{\circ}$
D. $119^{\circ}$

| Item Information | C-G.2.1.2 |
| :--- | :--- |
| Alignment | A |
| Answer Key | 1 |
| Depth of Knowledge | $65 \%$ (correct answer) |
| $p$-value A | $10 \%$ |
| $p$-value B | $9 \%$ |
| $p$-value C | $16 \%$ |
| $p$-value D | A. correct <br> B. misidentifies same-side exterior angles as having a difference of $45^{\circ}$ <br> C. recognizes that angles are supplementary but uses 200 <br> D. misidentifies same-side exterior angles as being congruent instead of <br> Supplementary |
| Option Annotations |  |

13. Concrete is poured to create a slab in the shape of a rectangular prism. The slab is 50 yards long, 1.5 yards wide, and 0.25 yard thick. How many cubic yards of concrete are needed to create the slab?
A. 18.75
B. 25.75
C. 155.25
D. 175.75

| Item Information | C-G.2.2.2 |
| :--- | :--- |
| Alignment | A |
| Answer Key | 1 |
| Depth of Knowledge | $12 \%$ (correct answer) |
| $p$-value A | $27 \%$ |
| $p$-value B | $45 \%$ |
| $p$-value C | $16 \%$ |
| $p$-value D | A. correct <br> B. determines perimeter using length and width and then multiplies the <br> Option Annotations <br> C. adds the given dimensions, then multiplies the sum by 3 <br> D. calculates the surface area |

14. Customers in two randomly selected groups at a yogurt shop are asked their preference of yogurt flavors. The responses for the customers in each group are summarized in the table below.

Customer Yogurt Flavor Preference

|  | Peach | Strawberry | Vanilla | Total |
| :--- | :---: | :---: | :---: | :---: |
| Group 1 | 40 | 25 | 10 | 75 |
| Group 2 | 50 | 10 | 15 | 75 |

Based on the information shown in the table, which statement best describes the preferences of the customers in the two groups?
A. In both groups, more customers prefer peach-flavored yogurt than either of the other two flavors.
B. In both groups, fewer customers prefer vanilla-flavored yogurt than either of the other two flavors.
C. In group 2, the same number of customers prefer strawberry-flavored yogurt and vanilla-flavored yogurt.
D. In group 1, more customers prefer either strawberry-flavored yogurt or vanilla-flavored yogurt than peach-flavored yogurt.

## Item Information

| Alignment | D-S.1.1 |
| :--- | :--- |
| Answer Key | A |
| Depth of Knowledge | 2 |
| $p$-value A | $79 \%$ (correct answer) |
| $p$-value B | $8 \%$ |
| $p$-value C | $7 \%$ |
| $p$-value D | $6 \%$ |
| Option Annotations | A. correct <br> B. selects a statement that is true for group 1 only <br> C. compares the 10 under Strawberry for Group 2 to the 10 under Vanilla for <br> Group 1 |
| D. does not recognize that more than half of Group 1 prefers Peach |  |

15. A team of 10 basketball players have their heights recorded to make a data set. The mean, median, mode, and range of the data set are recorded. Then, the height of the team's coach is included to make a new data set. The coach is shorter than all but one of the basketball players. Which measure must be the same when the coach's height is included?
A. mean
B. median
C. mode
D. range

## Item Information

\(\left.$$
\begin{array}{|l|l|}\hline \text { Alignment } & \text { D-S.2 } \\
\hline \text { Answer Key } & \text { D } \\
\hline \text { Depth of Knowledge } & 2 \\
\hline p \text {-value A } & 12 \% \\
\hline p \text {-value B } & 16 \% \\
\hline p \text {-value C } & 26 \% \\
\hline p \text {-value D } & 46 \% \text { (correct answer) } \\
\hline \text { Option Annotations } & \begin{array}{l}\text { A. does not consider that the coach's height could be different from the mean } \\
\text { height and would change the value of the mean }\end{array} \\
\hline\end{array}
$$ \begin{array}{l}B. does not consider that the fifth and sixth tallest players could be different <br>
heights and adding a height that is shorter than either of these heights to <br>

the data set would change the value of the median\end{array}\right\}\)| Coes not consider that the coach could be the same height as the shortest |
| :--- |
| player and that this height could be the new mode |

## PSSA MATHEMATICS GRADE 7

16. Some of the squares on the grid below are shaded.


One square on the grid is randomly selected. What is the probability that the square is not shaded?
A. $\frac{1}{36}$
B. $\frac{1}{30}$
C. $\frac{29}{36}$
D. $\frac{5}{6}$

## Item Information

| Alignment | D-S.3.2.2 |
| :--- | :--- |
| Answer Key | D |
| Depth of Knowledge | 2 |
| $p$-value A | $15 \%$ |
| $p$-value B | $17 \%$ |
| $p$-value C | $18 \%$ |
| $p$-value D | $50 \%$ (correct answer) |
| Option Annotations | A. determines probability using 1 randomly selected square out of 36 squares <br> B. determines probability using 1 randomly selected square out of 30 squares <br> that are not shaded |
| C. subtracts 1 randomly selected square from 30 squares that are not shaded |  |
| and determines probability using this difference out of 36 squares |  |

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## OPEN-ENDED QUESTION

17. Bella bought gardening materials from different stores.

At Garden Mart, Bella bought $g$ packets of geranium seeds, $m$ packets of marigold seeds, and $z$ packets of zinnia seeds. All of the plant seeds were on sale for half price. The expression shown below represents the total cost of the plant seeds Bella bought.

$$
\frac{1}{2}(2.48 g+1.74 m+1.96 z)
$$

A. Write an expression without parentheses that also represents Bella's total cost at Garden Mart.

At Plant World, Bella bought a hose and a shovel. The hose was priced at $\$ 29.68$, but Bella had a coupon for $x$ dollars off. The price of the shovel was $\$ 14.45$.
B. Write an expression to represent how much money, in dollars, Bella spent at Plant World.
17. Continued. Please refer to the previous page for task explanation.

Bella went to Yard Depot multiple times. Each time she was there, Bella bought a gardening hat and $y$ pairs of gardening gloves. The expression shown below represents the total amount of money, in dollars, Bella spent at Yard Depot.

$$
a(b y+c)
$$

C. Explain what $a, b$, and $c$ each mean in terms of the situation.

## Item-Specific Scoring Guideline

## \#17 Item Information

| Alignment | B-E.1 | Depth of Knowledge | 2 | Mean Score | 0.99 |
| :--- | :---: | :---: | :---: | :---: | :---: |

## Assessment Anchor this item will be reported under:

M07.B-E.1-Represent expressions in equivalent forms.

## Specific Anchor Descriptor addressed by this item:

M07.B-E.1.1-Use properties of operations to generate equivalent expressions.

## Scoring Guide

| Score | In this item, the student ... |
| :---: | :--- |
| $\mathbf{4}$ | Demonstrates a thorough understanding of representing expressions in equivalent forms by <br> correctly solving problems and clearly explaining procedures. |
| $\mathbf{3}$ | Demonstrates a general understanding of representing expressions in equivalent forms by <br> correctly solving problems and clearly explaining procedures with only minor errors or omissions. |
| $\mathbf{2}$ | Demonstrates a partial understanding of representing expressions in equivalent forms by <br> correctly performing a significant portion of the required task. |
| $\mathbf{1}$ | Demonstrates minimal understanding of representing expressions in equivalent forms. |
| $\mathbf{0}$ | The response has no correct answer and insufficient evidence to demonstrate any understanding <br> of the mathematical concepts and procedures as required by the task. Response may show only <br> information copied from the question. |

## Top-Scoring Student Response and Training Notes

| Score | Description |
| :---: | :--- |
| $\mathbf{4}$ | Student earns 4 points. |
| $\mathbf{3}$ | Student earns 3.0-3.5 points. |
| $\mathbf{2}$ | Student earns 2.0-2.5 points. |
| $\mathbf{1}$ | Student earns 0.5-1.5 points. <br> OR <br> Student demonstrates minimal understanding of representing expressions in equivalent forms. |
| $\mathbf{0}$ | Response is incorrect or contains some correct work that is irrelevant to the skill or concept <br> being measured. |

## Top-Scoring Response

Part A (1 point):
1 point for correct answer

| What? |  |
| :--- | :--- |
| $1.24 g+0.87 m+0.98 z$ | Why? |
| OR |  |
| $\frac{1}{2} \times 2.48 g+\frac{1}{2} \times 1.74 m+\frac{1}{2} \times 1.96 z$ |  |
| OR EQUIVALENT |  |

## Part B (1 point):

1 point for correct answer

| What? |  |
| :--- | :--- |
| $44.13-x$ |  |
| OR |  |
| $29.68-x+14.45$ |  |
| OR EQUIVALENT |  |

## Part C (2 points):

2 points for 3 correct and complete explanations
OR 1 point for 2 of 3 correct and complete explanations

| What? | Why? |
| :--- | :--- |
|  | Sample Explanation: <br> The $a$ represents the number of times Bella goes to Yard Depot. <br> The $b$ represents the price for each pair of gloves. <br> The $c$ represents the price for a gardening hat. |

## STUDENT RESPONSE

## Response Score: 4 points

17. Bella bought gardening materials from different stores.

At Garden Mart, Bella bought $g$ packets of geranium seeds, $m$ packets of marigold seeds, and $z$ packets of zinnia seeds. All of the plant seeds were on sale for half price. The expression shown below represents the total cost of the plant seeds Bella bought.

$$
\frac{1}{2}(2.48 g+1.74 m+1.96 z)
$$

A. Write an expression without parentheses that also represents Bella's total cost at Garden Mart.

$$
\frac{2.48 g}{2}+\frac{1.74 m}{2}+\frac{1.96 z}{2}
$$

The student has given a correct expression.

At Plant World, Bella bought a hose and a shovel. The hose was priced at $\$ 29.68$, but Bella had a coupon for $x$ dollars off. The price of the shovel was $\$ 14.45$.
B. Write an expression to represent how much money, in dollars, Bella spent at Plant World.

$$
29.68-x+14.45
$$

The student has given a correct expression.

PSSA MATHEMATICS GRADE 7
17. Continued. Please refer to the previous page for task explanation.

Bella went to Yard Depot multiple times. Each time she was there, Bella bought a gardening hat and $y$ pairs of gardening gloves. The expression shown below represents the total amount of money, in dollars, Bella spent at Yard Depot.

$$
a(b y+c)
$$

C. Explain what $a, b$, and $c$ each mean in terms of the situation. $A$ is the number of tim
visited Yard Depot.
$B$ is the price of one pair of gardening gloves.
$C$ is the price of one gardening hat.

The student has given 3 correct and complete explanations.

After you have checked your work, close your answer booklet and test booklet so your teacher will know you are finished.

## STUDENT RESPONSE

## Response Score: $\mathbf{3}$ points



## PART A



## PART B



## STUDENT RESPONSE

## Response Score: $\mathbf{2}$ points

17. Bella bought gardening materials from different stores.

At Garden Mart, Bella bought $g$ packets of geranium seeds, $m$ packets of marigold seeds, and $z$ packets of zinnia seeds. All of the plant seeds were on sale for half price. The expression shown below represents the total cost of the plant seeds Bella bought.

$$
\frac{1}{2}(2.48 g+1.74 m+1.96 z)
$$

A. Write an expression without parentheses that also represents Bella's total cost at Garden Mart.

$$
2.48 \mathrm{~g}+1.74 \mathrm{~m}+1.96 z \cdot 0.5
$$

The student has given an incorrect expression.

At Plant World, Bella bought a hose and a shovel. The hose was priced at $\$ 29.68$, but Bella had a coupon for $x$ dollars off. The price of the shovel was $\$ 14.45$.
B. Write an expression to represent how much money, in dollars, Bella spent at Plant World.

$$
\$ 29.68-x=\$ 14.45
$$

The student has given an incorrect answer.
17. Continued. Please refer to the previous page for task explanation.

Bella went to Yard Depot multiple times. Each time she was there, Bella bought a gardening hat and $y$ pairs of gardening gloves. The expression shown below represents the total amount of money, in dollars, Bella spent at Yard Depot.

$$
a(b y+c)
$$

C. Explain what $a, b$, and $c$ each mean in terms of the situation.
$\boldsymbol{a}=$ how many times Bella went to Yard Depot and bought something
$b=$ the price of one pair of gloves

$$
c=\text { the price of the gardening hat }
$$

The student has given 3 correct and complete explanations.

After you have checked your work, close your answer booklet and test booklet so your teacher will know you are finished.

## STUDENT RESPONSE

## Response Score: 1 point



## PART A



## PART B



## STUDENT RESPONSE

## Response Score: 0 points

17. Bella bought gardening materials from different stores.

At Garden Mart, Bella bought $g$ packets of geranium seeds, $m$ packets of marigold seeds, and $z$ packets of zinnia seeds. All of the plant seeds were on sale for half price. The expression shown below represents the total cost of the plant seeds Bella bought.

$$
\frac{1}{2}(2.48 g+1.74 m+1.96 z)
$$

A. Write an expression without parentheses that also represents Bella's total cost at Garden Mart.

$$
\frac{1}{2}(2.48+1.740+1.960)
$$ add all together and get $\$ 6.18$ Dollars

$$
\left.\frac{1}{2} 2.48+1.74+1.96\right) \leftarrow \text { add }
$$

At Plant World, Bella bought a hose and a shovel. The hose was priced at $\$ 29.68$, but Bella had a coupon for $x$ dollars off. The price of the shovel was $\$ 14.45$.
B. Write an expression to represent how much money, in dollars, Bella spent at Plant World.


The coupon was 15.23 Dollars off when she bought the shovel.

The student has given an incorrect answer.

Go to the next page to finish question 17.


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17. Continued. Please refer to the previous page for task explanation.

Bella went to Yard Depot multiple times. Each time she was there, Bella bought a gardening hat and $y$ pairs of gardening gloves. The expression shown below represents the total amount of money, in dollars, Bella spent at Yard Depot.

$$
a(b y+c)
$$

C. Explain what $a, b$, and $c$ each mean in terms of the situation.
(A) means the Fraction
(BY) means the numbers You add
(C) mean the other number Yo
add like the by number.

The student has given no correct explanations.

After you have checked your work, close your answer booklet and test booklet so your teacher will know you are finished.

## MATHEMATICS—SUMMARY DATA

## MULTIPLE-CHOICE

$\left.\begin{array}{|c|c|c|c|c|c|c|c|}\hline \begin{array}{c}\text { Sample } \\ \text { Number }\end{array} & \text { Alignment } & \text { Answer Key } & \begin{array}{c}\text { Depth of } \\ \text { Knowledge }\end{array} & \begin{array}{c}\text { p-values } \\ \text { A }\end{array} & \text { p-values } & \text { B-values } & \boldsymbol{p} \text {-values } \\ \text { C }\end{array}\right]$

## OPEN-ENDED

| Sample <br> Number | Alignment | Points | Depth of <br> Knowledge | Mean Score |
| :---: | :---: | :---: | :---: | :---: |
| 17 | B-E.1 | 4 | 2 | 0.99 |



## PSSA Grade 7 Mathematics Item and Scoring Sampler

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[^0]:    1 The permission to copy and/or use these materials does not extend to commercial purposes.

[^1]:    2 All $p$-value percentages listed in the item information tables have been rounded.

